

1 Performance and limitations of linkage-disequilibrium-based 2 methods for inferring the genomic landscape of recombination and 3 detecting hotspots: a simulation study

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7 8 9 **Abstract**

10
11 Knowledge of recombination rate variation along the genome provides important
12 insights into genome and phenotypic evolution. Population genomic approaches offer an
13 attractive way to infer the population-scaled recombination rate $\rho=4N_e r$ using the linkage
14 disequilibrium information contained in DNA sequence polymorphism data. Such methods
15 have been used in a broad range of plant and animal species to build genome-wide
16 recombination maps. However, the reliability of these inferences has only been assessed
17 under a restrictive set of conditions. Here, we evaluate the ability of one of the most widely
18 used coalescent-based programs, *LDhelmet*, to infer a genomic landscape of recombination
19 with the biological characteristics of a human-like landscape including hotspots. Using
20 simulations, we specifically assessed the impact of methodological (sample size, [phasing](#)
21 [errors](#), block penalty) and evolutionary parameters (effective population size (N_e),
22 [demographic history](#), mutation to recombination rate ratio) on inferred map quality. We report
23 reasonably good correlations between simulated and inferred landscapes, but point to
24 limitations when it comes to detecting recombination hotspots. False positive and false
25 negative hotspots considerably confound fine-scale patterns of inferred recombination under
26 a wide range of conditions, particularly when N_e is small and the mutation/recombination rate
27 ratio is low, to the extent that maps inferred from populations sharing the same recombination
28 landscape appear uncorrelated. We thus address a message of caution for the users of these
29 approaches, at least for genomes with complex recombination landscapes such as in humans.

30 31 **Key words**

32 Population-scaled recombination rate, LDhelmet, simulations, linkage disequilibrium,
33 recombination hotspots

36 Introduction

37

38 Recombination is highly conserved among sexually reproducing species of
39 eukaryotes. This fundamental mechanism of meiosis is essential for the proper segregation
40 of homologous chromosomes during the reductional division. Recombination involves
41 crossing over events (CO) that play a crucial evolutionary role by allowing genetic mixing and
42 generating new combinations of alleles (Baudat and de Massy 2007; Cromie et al. 2001;
43 Capilla et al. 2016). Measuring the rate at which recombination occurs and the magnitude of
44 its variation along the genome has important implications for fundamental research in
45 molecular biology and evolution (Stapley et al. 2017), but also for applied genomics such as
46 genome-wide association studies (GWAS) (Morris et al. 2013; Hunter et al. 2016). Several
47 approaches have been developed to reconstruct genome-wide recombination maps (reviewed
48 in Peñalba and Wolf 2020). Cytological methods, like ChIP-seq, target protein-DNA
49 complexes directly involved in the formation of double-strand breaks (DSB) and CO during
50 meiosis (Pratto et al. 2014). Gamete typing methods analyse the meiotic products of a diploid
51 individual (reviewed in (Carrington and Cullen 2004; Dréau et al. 2019; Sun et al. 2019).
52 Methods based on pedigree analysis reconstruct the gametic phase from patterns of allele
53 inheritance in bi-parental crosses (Lander et Green 1987; Kong et al. 2002; Kodama et al.
54 2014; Rastas 2017). All these approaches have the advantage of providing direct estimates
55 of the recombination rate. However, by focusing on CO that occurred in a few individuals or
56 families across one or a couple of generations, they remain intrinsically limited in resolution
57 due to the small number of recombination events that occur per chromosome per generation
58 (Clark et al. 2010; Peñalba and Wolf 2020).

59 Another type of approach uses genome sequence data from population samples to
60 take advantage of the large number of recombination events that have occurred during the
61 history of the considered population. Instead of directly observing crossover products, these
62 methods detect the footprints left by historical recombination events on patterns of haplotype
63 segregation and linkage disequilibrium (LD) (reviewed in Stumpf and McVean 2003). The
64 recombination rate and its variation across the genome are inferred via coalescent-based
65 analysis of DNA sequence polymorphism data (Chan et al. 2012; Kamm et al. 2016; Li and
66 Stephens 2003.; McVean et al. 2004; Spence and Song 2019). The resulting LD maps have
67 been widely used to evaluate the genomic impact of natural selection and admixture, and to
68 perform genome-wide association studies (GWAS) (e.g. Chan et al. 2012; The International
69 HapMap Consortium 2007). These approaches provide an accessible and attractive way of
70 describing recombination landscapes - *i.e.* the variation of recombination rates along the

71 genome - particularly in non-model taxa where direct methods are often difficult to implement
72 (Auton et al. 2012; 2013; Melamed-Bessudo et al. 2016; Shanfelter et al. 2019; Singhal et al.
73 2015; Shield et al., 2020).

74 Direct and indirect methods have revealed considerable variation in recombination
75 rate at different scales along the genome, particularly in vertebrates. At a large scale (of the
76 megabase order), recombination tends to be concentrated in subtelomeric regions compared
77 to centromeric and centro-chromosomal regions, a pattern shared among many species of
78 plants and animals (Auton et al. 2012; Melamed-Bessudo et al. 2016; Capilla et al. 2016;
79 Danguy des Déserts et al. 2021; Haenel et al. 2018). At a finer scale (of the kilobase order),
80 recombination events often cluster within small regions of about 2 kb, called recombination
81 hotspots (Choi and Henderson 2015; Kim et al. 2007; Mancera et al. 2008; Myers et al. 2005;
82 Singhal et al. 2015; Shanfelter et al. 2019; Schield et al., 2020). Two distinct regulatory
83 systems of recombination hotspot location have been described to date, with major
84 implications on the evolutionary dynamics of recombination landscapes. In passerine birds
85 (Singhal et al. 2015), dogs (Axelsson et al. 2012; Auton et al. 2013) and some teleost fishes
86 (Baker et al., 2017; Shanfelter et al., 2019), recombination hotspots tend to be found in CpG-
87 islands / promoter-like regions, and are highly conserved between closely-related species
88 (Singhal et al. 2015). In contrast, in humans (Myers et al. 2005; 2010), apes (Auton et al.
89 2012 ; Great Ape Genome Project 2016) and mice (Booker et al. 2017), hotspot location is
90 directed by the PRDM9 protein, which binds specific DNA motifs and triggers DSBs (Oliver et
91 al. 2009; Baudat et al. 2010; Myers et al. 2010; Parvanov et al. 2010; Grey et al. 2018). In
92 these taxa, hotspots are mostly located away from genes (Auton et al., 2012; Baker et al.
93 2017), and show little or no conservation between closely related species (Myers et al. 2005,
94 2010; Auton et al. 2012; Booker et al. 2017) due to self-destruction by gene conversion and
95 rapid turnover of PRDM9 alleles (Coop and Myers 2007; Lesecque et al. 2014; Latrille et al.
96 2017).

97 Population-based inference methods aim to infer the population recombination rate ρ
98 $= 4N_e r$, r being the per generation, per bp recombination rate and N_e the effective population
99 size (Stumpf et McVean 2003). The ρ parameter reflects the density of population
100 recombination events that segregate in polymorphism data, integrated across time and
101 lineages. Several programs have been developed for reconstructing LD-maps (reviewed in
102 (Peñalba and Wolf 2020; including PHASE: Li and Stephens 2003, LDhat: McVean et al. 2004,
103 LDhelmet: Chan et al. 2012, LDpop: Kamm et al. 2016, and pyrho: Spence and Song 2019),
104 which use the theory of coalescence with recombination to model the complex genealogies of
105 samples stored in the underlying ancestral recombination graph (Griffiths et al. 1997; Arenas,

106 2013). The most popular family of LD-based methods, comprising LDhat (McVean et al. 2004)
107 and its improved version LDhelmet (Chan et al. 2012) (see a literature survey in
108 [Supplementary Figure S1](#)), implement a pairwise composite likelihood method under a
109 Bayesian framework using a reversible jump Markov Chain Monte Carlo (rjMCMC) algorithm.
110 They have been used for building fine scale LD-based maps in a broad range of animal taxa
111 including humans (McVean et al. 2004), dogs (Axelsson et al. 2012; Auton et al. 2013), fruit
112 flies (Chan et al. 2012), finches (Singhal et al. 2015), honeybees (Wallberg et al. 2015),
113 sticklebacks (Shanfelter et al. 2019) and rattlesnakes (Schield et al., 2020). In some species,
114 inferred LD-based maps have been validated by comparison with recombination maps
115 obtained using direct approaches, confirming their overall good quality (McVean et al. 2004;
116 Chan et al. 2012; Singhal et al. 2015; Booker et al. 2017; Shanfelter et al. 2019). However, as
117 genetic and LD-based maps greatly differ in their resolution (pedigree-based inference provide
118 resolution of about 1 cM, while population-based methods can infer recombination events at
119 the kilobase scale, Peñalba and Wolf 2020), such comparisons do not provide qualitative
120 information on the reliability of inferred fine-scale variation and hotspots detection. Moreover,
121 the heterogeneity of studies in terms of taxonomy, genetic diversity, demography, sample
122 size, and software parameters, among other things makes it difficult to appreciate the
123 performance and the possible weaknesses of LD-based methods. For these reasons, the
124 reliability and conditions of application of LD-based methods are still poorly understood and
125 need to be more thoroughly characterised, considering the growing importance of these tools.

126 The power and sensitivity of LDhat and LDhelmet have been tested by simulations
127 aiming to evaluate the influence of switch error in haplotype phasing (Singhal et al. 2015;
128 Booker et al. 2017), the amount of polymorphism, and the intensity of recombination hotspots
129 (Singhal et al. 2015). These studies simulated simple recombination landscapes assuming
130 either homogeneous recombination rates or a few, well-defined hotspots contrasting with a
131 low-recombination background (McVean et al. 2004; Auton and McVean, 2007; Chan et al.
132 2012; Singhal et al. 2015; Booker et al. 2017; Shanfelter et al. 2019; Schield et al., 2020). Real
133 recombination landscapes that were characterised with a fine-scale resolution such as in
134 humans, however, appeared to be more complex and involve a continuous distribution of
135 recombination hotspot density and intensity across genomic regions. This complexity has not
136 been taken into account so far in benchmarking studies assessing the performance of LD-
137 map reconstruction methods. We thus lack a comprehensive picture of the ability of these
138 methods to properly recover the biological characteristics of human-like recombination
139 landscapes interspersed with hotspots. In particular, the proportion of the inferred
140 recombination hotspots that are correct, and the proportion of true hotspots that are missed,

141 have not yet been quantified under a biologically realistic scenario. These are crucial quantities
142 to properly interpret and use reconstructed LD-maps in genomic research.

143 In this work, we specifically assessed the performance of the LDhelmet program to
144 detect hotspots while assuming a biologically realistic recombination landscape. *We evaluated*
145 *the influence of methodological parameters including sample size, phasing errors and block*
146 *penalty, the impact of the population demographic history including its long-term effective size*
147 *and the occurrence of bottleneck and admixture events, and finally the effect of the mutation*
148 *to recombination rate ratio.* We also considered different definitions of a recombination hotspot
149 relative to its background recombination rate, with the aim of improving the sensitivity of the
150 analysis. We identified the conditions in which LD-based inferences can provide an accurate
151 mapping of hotspots, and the parameters that negatively affect the sensitivity and specificity
152 of their detection across biologically realistic recombination landscapes.

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156 **Results**

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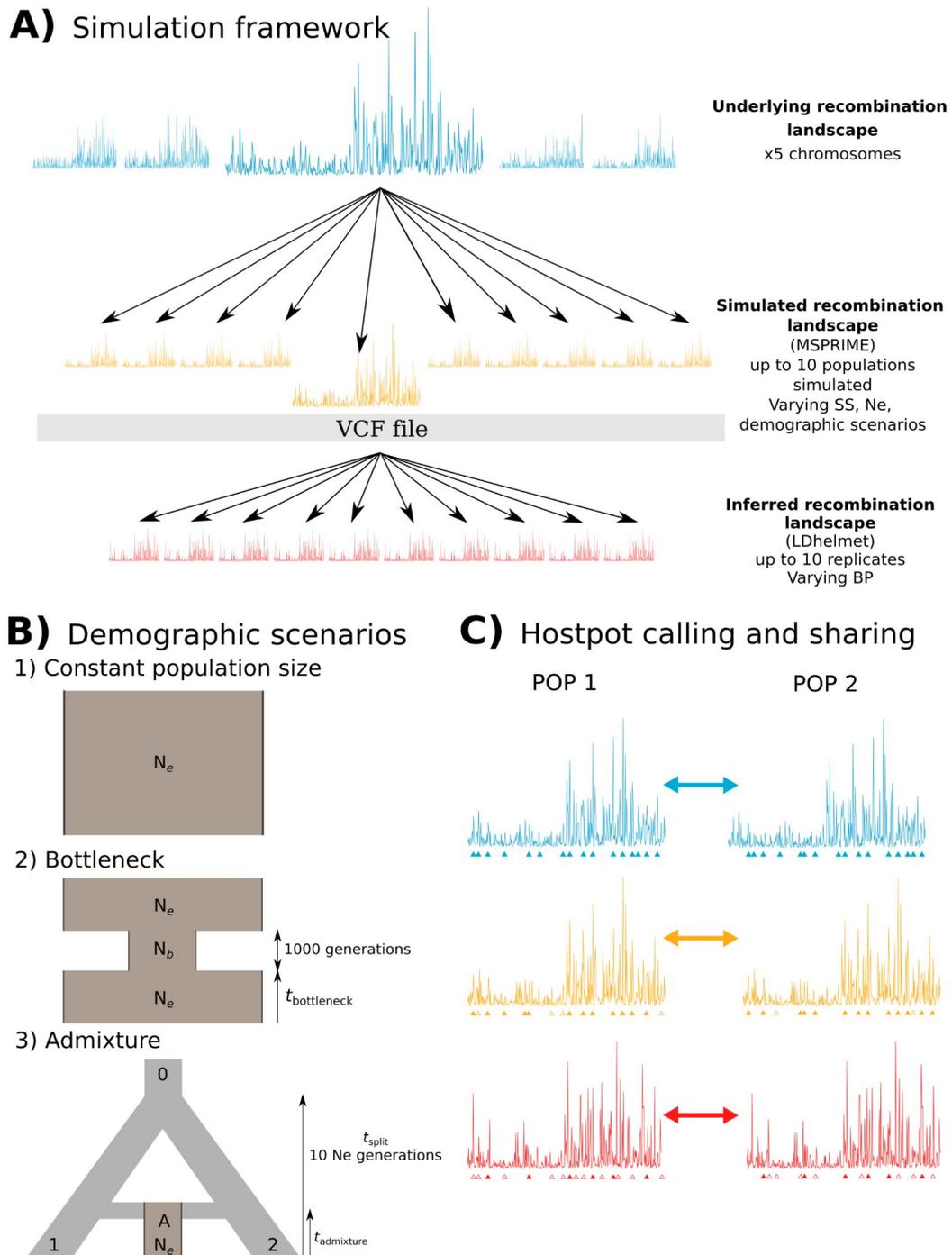
158 ***Recombination landscape modelling***

159 Five realistic, heterogeneous recombination landscapes (referred to as “underlying
160 landscapes” throughout) of 1Mb length were built using the human genome high resolution
161 map of meiotic DSB from Pratto et al. (2014). In order to mimic both broad and fine-scale
162 variation in the recombination rate parameter “ r ”, the first and second half of each landscape
163 were drawn from a gamma distribution with mean 1 cM/Mb and 3 cM/Mb, respectively, and
164 parameters fitted from Pratto et al. (2014) (1-500,000bp: shape=rate=0.1328; 500,001pb-
165 1Mb: shape=0.1598, rate=0.0532). Accordingly, the 5 recombination landscapes generated
166 (Supplementary Figure S2) showed broad-scale differences in recombination peak intensity,
167 with less elevated recombination peaks in the first half compared with the second half of each
168 chromosome. At a fine scale, recombination was concentrated in numerous peaks resembling
169 human recombination hotspots, with about 85% of the recombination concentrated in 15% of
170 the genome. The map lengths in recombination units were about 0.02 Morgan (Supplementary
171 Figure S2, S4).

172 Population-scaled recombination landscapes simulated under a constant effective
173 population size (hereafter called “simulated landscapes”) were generated in 10 replicates for
174 the five underlying landscapes, using coalescent simulations with a mutation rate $\mu=10^{-8}$
175 and 4 combinations of sample sizes (SS=10 or 20) and effective population sizes ($N_e=25,000$

176 or 250,000) (Figure 1A, Supplementary Figure S3A). The map lengths of simulated
177 landscapes were a little shorter than the underlying landscapes (about 0.015-0.018 Morgan),
178 reflecting the occasional occurrence of more than one recombination event between two
179 adjacent SNPs during the simulated coalescent histories (Supplementary Figure S4). These
180 simulated landscapes were also highly correlated with the underlying landscapes for each
181 combination of parameters (Spearman's rank correlation > 0.8 using a 500bp resolution level),
182 showing that the coalescent history has not resulted in a substantial loss of information about
183 recombination rate variation across the underlying landscape. As expected from the $\theta=4N_e\mu$
184 values used in our simulations ($\theta = 0.001$ and 0.01 for $N_e = 25,000$ and $250,000$, respectively),
185 the SNPs density of the large N_e populations was about one order of magnitude higher than
186 for smaller N_e populations (Supplementary Figure S5).

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Figure 1. Simulation and hotspot calling protocols. **A)** Simulation framework. Five different underlying recombination landscapes were generated based on human empirical data. These five landscapes can either be considered as different regions from distinct chromosomes within a same species, or as orthologous regions of a same chromosome in different species. From these underlying landscapes, up to 10 recombination landscapes were simulated with MSPRIME 0.7.4 under various demographic scenarios, varying the effective population size (i.e. $N_e=25,000, 100,000, 250,000$) and the sample size (i.e. $SS=10, 20$), to generate a VCF file for each simulated population. The VCF files were then used to infer the local population recombination rates using LDhelmet 1.19 setting the block penalty to $BP = 5, 10$ or 50 . Up to

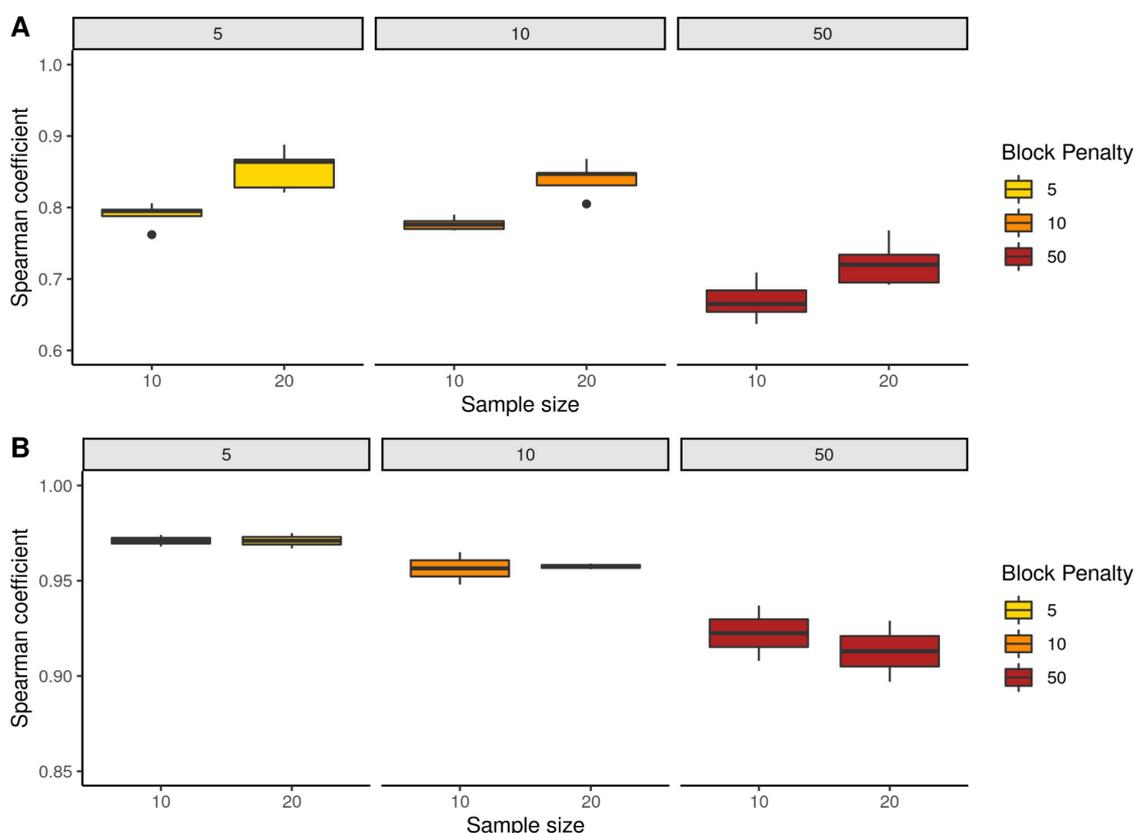
198 10 replicates per simulated population were analysed with LDhelmet. **B)** Demographic
199 scenarios. Three demographic scenarios were simulated with MSPRIME: 1) Constant
200 population size, varying the N_e of the simulated population; 2) Bottleneck event, varying the
201 age of the bottleneck (i.e. 500, 5000, 50000) and the N_e of the population during the bottleneck
202 (i.e. $N_b=2500, 25,000$), and setting the duration of the bottleneck to 1000 generations; 3)
203 Admixture event, varying the age of the admixture event (i.e. 500, 5000, 50000), and setting
204 the time of the split of the ancestral population into two populations $10 \cdot N_e$ generations ago.
205 **C)** Hotspot calling and sharing. Hotspots in the underlying (blue), simulated (orange) and
206 inferred (red) landscapes were defined as 2.5 kb-windows with a local recombination rate X
207 times as high as the averaged recombination rate of the 50 kb flanking regions. Several
208 threshold values were used to call the hotspots (i.e. $X=2.5, 5, 10$). The location of hotspots
209 was compared between populations (that share or not the same underlying landscape), to
210 compute the proportion of shared hotspots. Triangles below each landscape represent called
211 hotspots, with filled triangles indicating shared hotspots, and empty triangles hotspots that are
212 not shared with the compared landscape. In this example, the two compared populations
213 share the same underlying landscape, meaning that all the hotspots are shared between them
214 (all blue triangles are filled). The two simulated landscapes with independent coalescent
215 histories share most of these hotspots, while the two landscapes inferred with LDhelmet share
216 a smaller fraction of them, due to the additional inference step.

217

218 ***Methodological parameters affecting LDhelmet performance***

219 Population-scaled recombination rates (ρ) were inferred from the simulated
220 polymorphism datasets using the program LDhelmet (Chan et al. 2012) (referred to as
221 “inferred landscapes” throughout). The effect of sample size and landscape resolution level
222 were assessed for a constant effective population size ($N_e=25,000$) using 10 or 20 diploid
223 individuals (SS=10 or 20) and three block penalty (BP) values (BP=5, 10 or 50), which
224 inversely determine the number of allowed changes in ρ value within windows of 50
225 consecutive SNPs (Figure 1A, Supplementary Figure S3A). Underlying and simulated
226 landscapes were converted into population-scaled recombination rates ($\rho=4N_e r$), and each
227 underlying, simulated and inferred maps was smoothed using 500bp (i.e. the underlying
228 landscape resolution level) and 2500bp windows (i.e. a resolution level better suited to the
229 SNP density in our low- N_e simulations). The 10 simulated and inferred replicates of each
230 SS/BP condition were averaged to perform landscapes comparisons. Overall, local
231 recombination rates tended to be overestimated by LDhelmet, no matter the value used for
232 SS and BP, but this was especially observed when the local ρ was either very low ($\rho < 10^{-4}$)
233 or very high ($\rho > 10^{-2}$) (Supplementary Figure S6, panels A-F). The mean inferred map
234 lengths calculated across replicates varied substantially among tested conditions (0.017-
235 0.125 M), reaching up to 6 times the length of simulated maps in low SS and BP conditions
236 (i.e. SS = 10, BP = 5, 10, Supplementary Figure S4, upper panel). A BP value of 50 produced

237 very smooth recombination maps, which did not capture fine-scale variation in recombination
 238 rate. By contrast, maps inferred with BP=5 or BP=10 were visually similar and better reflected
 239 the fine-scale variation of the underlying landscapes (Supplementary Figure S7A). Spearman
 240 rank correlation coefficient between the mean simulated and inferred landscapes was reduced
 241 when SS were small (Figure 2A). Replicate runs of LDhelmet showed a strong consistency,
 242 as revealed by elevated correlations among the 10 replicate landscapes inferred from the
 243 same simulated landscape, whatever the SS and BP values being tested (Spearman's rho >
 244 0.89, Figure 2B).
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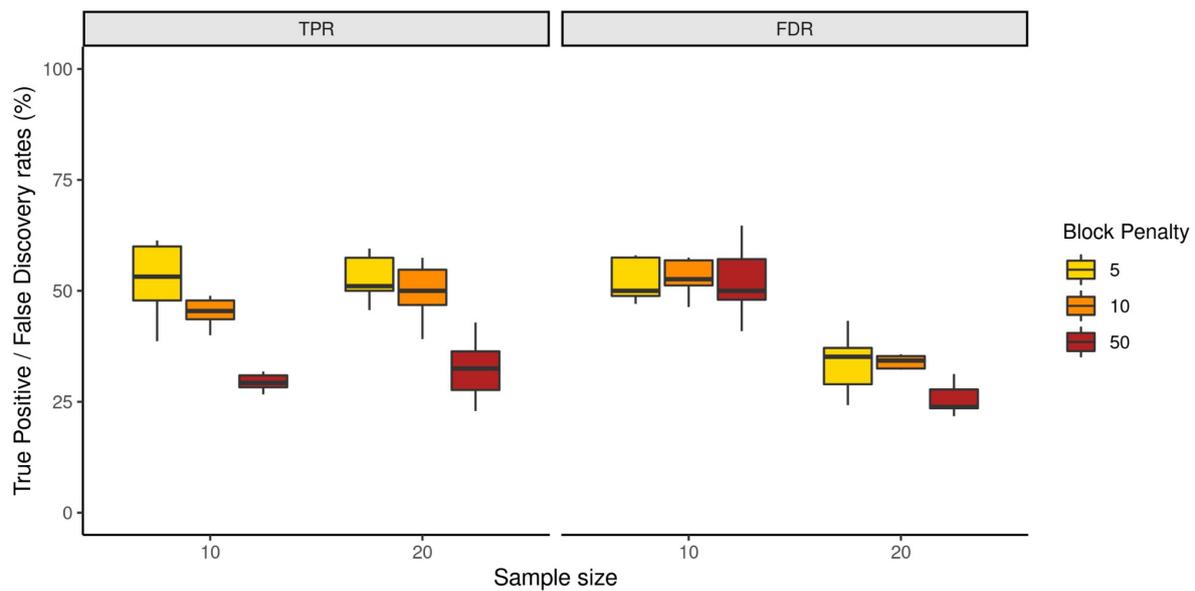


246
 247 **Figure 2.** Performance (A), and repeatability (B) of LDhelmet as a function of the different
 248 parameters tested (i.e. N_e , SS, BP). The N_e of the simulated population is 25,000, the sample
 249 size is shown on the x axis (i.e. SS=10 or 20), and the LDhelmet BP values shown in color
 250 correspond to the different panels (i.e. BP=5, 10 or 50). **A)** Spearman correlation coefficients
 251 between the mean simulated and the mean inferred landscape calculated across ten
 252 replicates for each of five underlying landscapes (Supplementary Figure S3A). **B)** Mean
 253 pairwise Spearman correlation coefficients calculated between the 10 replicates of inferred
 254 landscapes from simulated populations sharing the same underlying landscape (i.e.
 255 Supplementary Figure S3B).
 256

257 Recombination hotspots of the underlying, simulated and inferred landscapes were

258 called using three different threshold values commonly used in the literature (*i.e.* local
259 recombination rate at least 2.5, 5 or 10 times higher than the background rate). True/False
260 positives/negatives rates and discovery rates (TPR, FPR, TDR, FDR, TNR, FNR) were
261 computed under each tested condition. The hotspot detection threshold ratio of 10 between
262 the focal and flanking positions appeared too stringent and yielded a very small number of
263 called hotspots (Supplementary Figure S8). Using a less conservative threshold ratio of 5, we
264 detected 4 to 8 hotspots per Mb in the simulated landscapes, and 5 to 20 per Mb in the inferred
265 landscapes. These numbers reached 40-50 and 20-50 per Mb, respectively, when a threshold
266 of 2.5 was used. Irrespective of the chosen threshold, the number of inferred hotspots tended
267 to be overestimated, notably when SS was small (Supplementary Figure S8). The 2.5
268 threshold was used for the remaining analysis as it reduced the variance in the number of
269 called hotspots due to a higher call rate. The sensitivity (or TPR) of LDhelmet was medium,
270 since depending on the SS and the BP used, between 29.4% and 52.7% of the simulated
271 hotspots were inferred as such. The TPR was higher for small BP values (*i.e.* 5 or 10), but
272 relatively insensitive to the SS value (Figure 3 left panel, Supplementary Figure S9A). The
273 proportion of false hotspot calls (FDR, *i.e.* inferred hotspots corresponding to non-hotspot
274 windows in the simulated maps) ranged between 25.6% and 52.9%, and was higher for SS
275 = 10, without major differences between the BP values tested (Figure 3 right panel,
276 Supplementary Figure S9B and C). No significant difference in the correlation between
277 simulated and inferred landscapes was found between the first half of the chromosome with
278 a mean r of 1 cM/Mb (referred to as the “cold” region) and the last half with a mean r of 3 cM/Mb
279 (the “hot” region). This was also true for the TPR and the FDR, whatever the hotspot detection
280 threshold used (*i.e.* 2.5 or 5) (Student test, $p > 0.05$).

281



282

283 **Figure 3.** Hotspot detection. True positive (TPR, left panel) and false discovery (FDR, right
 284 panel) rates of inferred, as compared to simulated hotspots, called using a detection threshold
 285 of 2.5, for different sets of methodological parameters. The sample size parameter is shown
 286 on the x axis (i.e. 10 or 20), the block penalty (i.e. 5, 10, 50) is shown in color, and the N_e of
 287 the populations simulated is 25,000. See full results in Supplementary Figure S9.

288

289 To assess the impact of phasing errors on LDhelmet performance, the phase
 290 information was first removed from the whole VCF of the simulated landscapes for two
 291 replicate populations simulated with a constant N_e of 250,000 and a SS of 20. Statistical
 292 phasing performed with Shapeit 4.2.2 (Delaneau et al. 2019) resulted in a 6.7% average
 293 phasing error. We then introduced random phasing errors in the simulated VCFs with rates
 294 ranging from 2 to 10%, before inferring ρ with a BP value of 5. As the phasing error rate
 295 increased, Spearman rank correlation coefficients between simulated and inferred landscapes
 296 slightly decreased below the value obtained with perfectly phased data (Supplementary Figure
 297 S10A). Hotspot calling performance assessed with TPR and FDR was also negatively
 298 impacted by phasing errors (Supplementary Figure S10B).

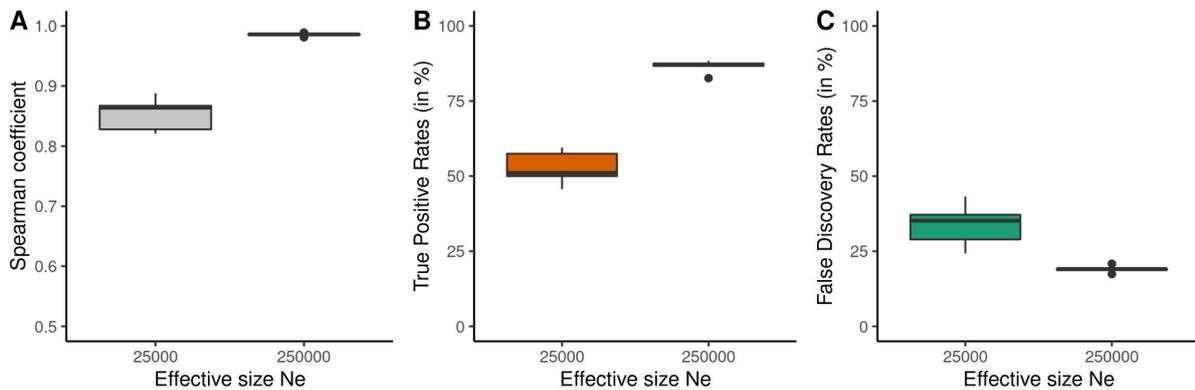
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300 **Demographic and evolutionary parameters affecting LDhelmet** 301 **performance**

302 Methodological parameters were then set to SS=20 individuals and BP=5 - a trade-off
 303 optimising the balance between TPR and FDR - to focus on the effect of N_e on the quality of
 304 the LD inferences. When the simulated effective population size was large (i.e. 250,000, as
 305 compared to 25,000), the inferred map length was closer to the expected value of 0.02 M
 306 (Supplementary Figure S4, lower panels) and the local recombination rate tended to be less

307 overestimated (Supplementary Figure S6, panels G-L). A larger N_e also significantly increased
308 the correlation between simulated and inferred landscapes (Figure 4A, Supplementary Figure
309 S11), increased the TPR and decreased the FDR (Figure 4B, C).

310



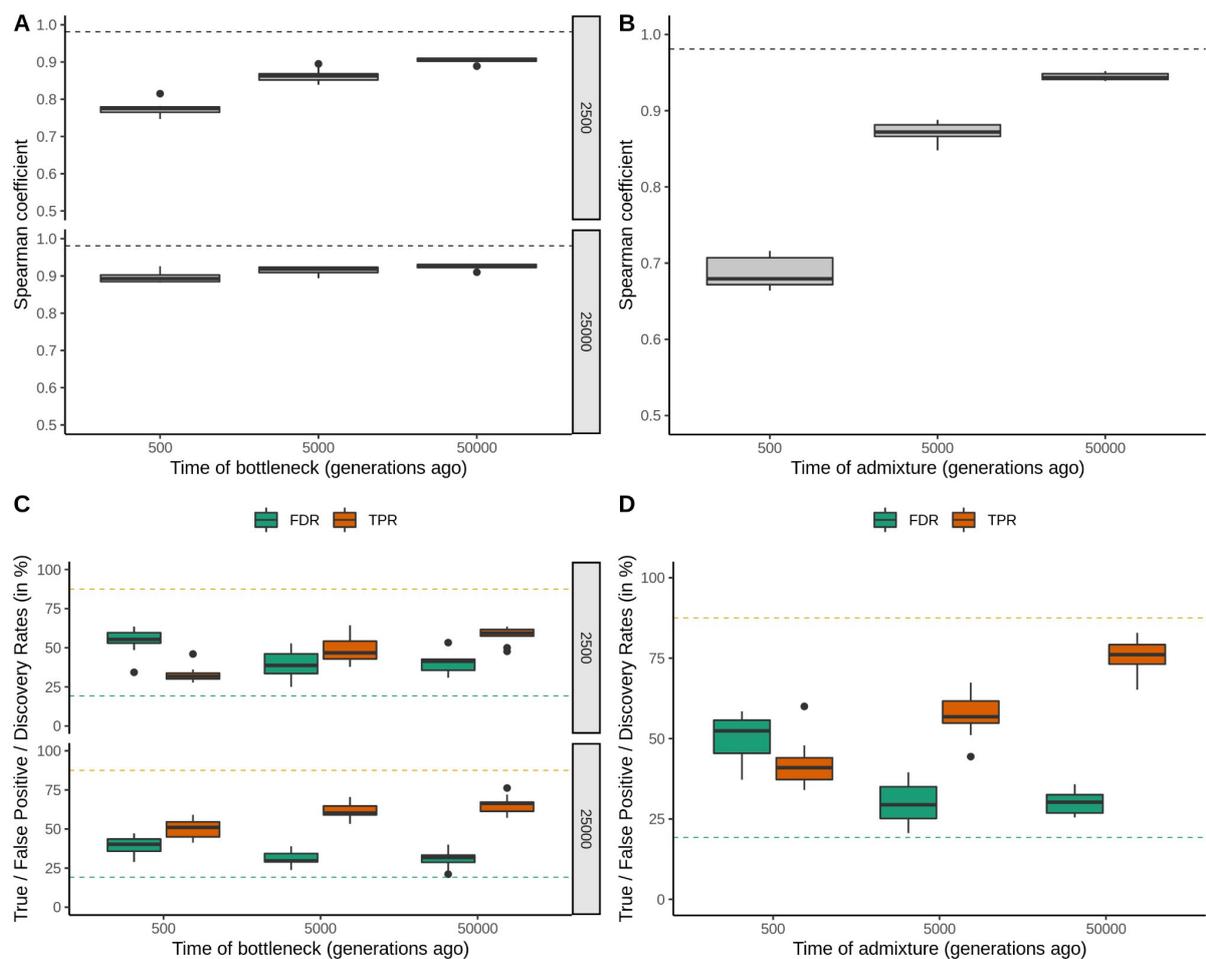
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312 **Figure 4.** Effect of the effective population size parameter (N_e) on recombination rate
313 inference and hotspot detection. **A)** Spearman correlation coefficients between simulated and
314 inferred landscapes as a function of N_e (SS = 20, BP = 5). **B)** and **C)** True positive (TP) and
315 false discovery (FD) rates of inferred, as compared to simulated hotspots, called using a
316 detection threshold of 2.5, as a function of N_e (SS = 20, BP = 5). See full results in
317 Supplementary Figure S9 and S11.

318

319 We then assessed the impact of non-equilibrium demographic histories. Populations
320 undergoing bottleneck or admixture events of various ages were simulated, with the N_e of the
321 ancestral and present-day populations set to 250,000, the SS to 20, and making other
322 demographic parameters vary (*i.e.* t_b , N_b , t_a , Figure 1B, see Materials and Methods). These
323 demographic scenarios generally had a negative impact on the quality of the reconstructions
324 (using a BP of 5), as compared to constant-size populations (Figure 5). The correlation
325 between simulated and inferred maps decreased with the strength of the bottleneck (*i.e.* with
326 lower N_b), and with the recentness of bottleneck and admixture events (Figure 4A, B). In the
327 same way, TPR and FDR were degraded as compared to constant-size population scenarios
328 (Figure 4C, D), particularly for young events.

329



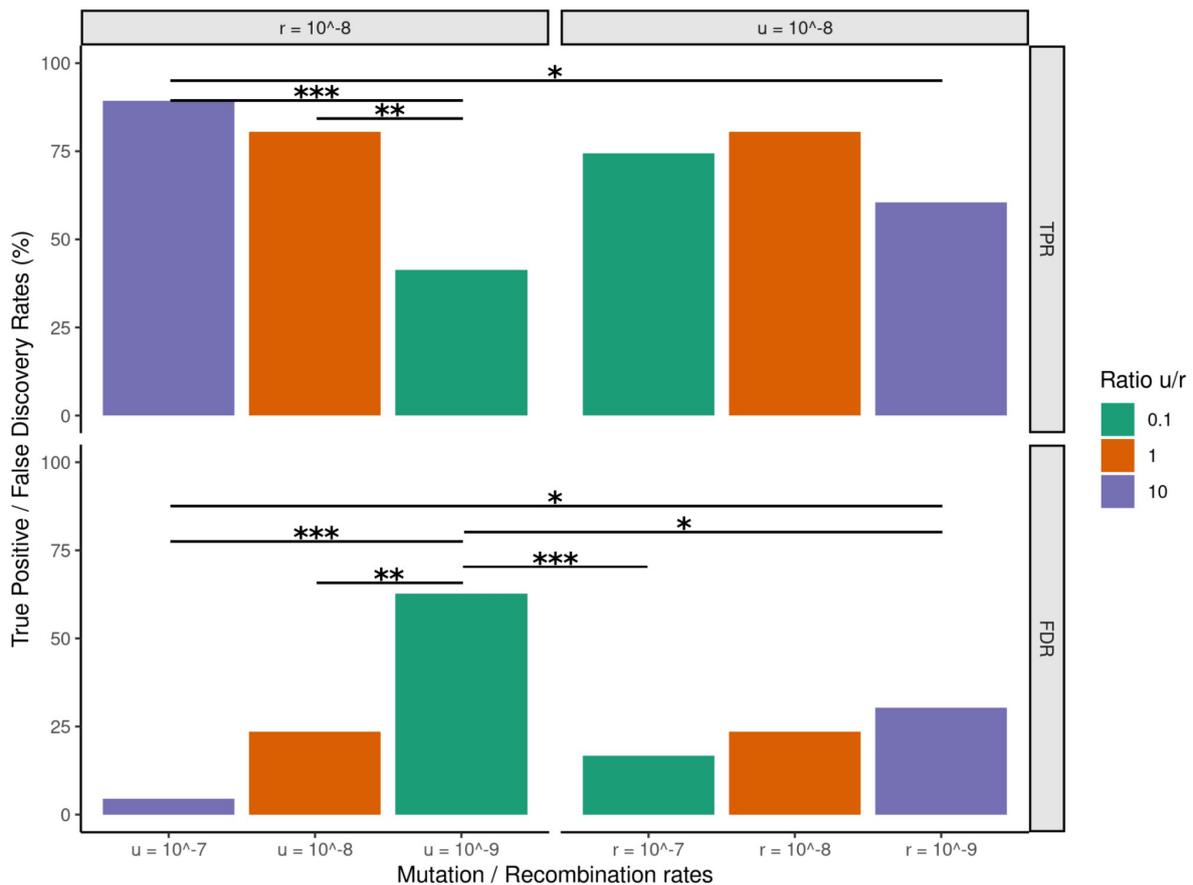
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331 **Figure 5.** Influence of bottleneck (left panels A and C) and admixture (right panels B and D)
 332 events on recombination rate inference and hotspot detection. Spearman correlation
 333 coefficients between simulated and inferred landscapes are shown as a function of the age of
 334 the bottleneck event and the strength of the bottleneck (i.e. N_b , the N_e value during the 1000
 335 generations of the bottleneck) (A), and as a function of the age of the admixture event (B).
 336 True positive (TP, in orange) and false discovery (FD, in green) rates of hotspots called using
 337 a detection threshold of 2.5, as a function of the time of the bottleneck event and the strength
 338 of the bottleneck (C), and as a function of the time of the admixture event (D). Dashed lines
 339 correspond to averaged Spearman's rho, TPR and FDR values in populations that did not
 340 experience bottleneck or admixture events.

341

342 The influence of species-specific evolutionary parameters such as the mutation and
 343 recombination rates was assessed by generating coalescent simulations under two additional
 344 underlying landscapes using a ten times higher (i.e. 20 cM/Mb) and a ten times lower (i.e. 0.2
 345 cM/Mb) average recombination rate, and three different mutation rates (i.e. 10^{-9} , 10^{-8} and
 346 10^{-7}). The μ/r ratio under these 6 simulated conditions thus equalled 0.1, 1 or 10. For all
 347 conditions, Spearman's rank correlation between the mean simulated and the mean inferred
 348 landscapes was greater than 0.9, except when μ equalled 10^{-9} (Spearman's rho ≈ 0.7 ,

349 Supplementary Table S1). An increased μ/r ratio improved the ability to detect hotspots when
 350 r was fixed to 10^{-8} , with a higher TPR (up to $>80\%$) and a lower FDR ($<5\%$) when μ increased
 351 (prop.test, p-value < 0.05 , Figure 6, threshold 5 in Supplementary Figure S12). The μ/r ratio
 352 did not affect the performances the same way when μ was fixed to 10^{-8} : a μ/r ratio of 10 (r
 353 $= 10^{-9}$) yielded lower TPR ($< 60\%$) and higher FDR ($> 25\%$) than a ratio of 1 or 0.1, although
 354 these trends were not significant (prop.test, p-value > 0.05 , Figure 6, threshold 5 in
 355 Supplementary Figure S12).
 356



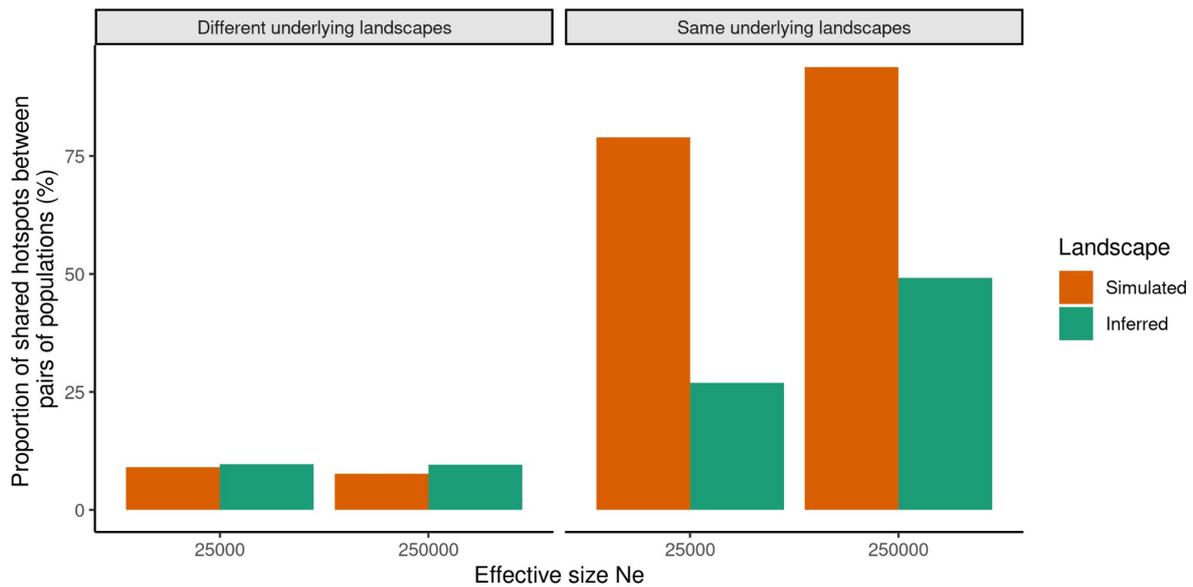
357
 358 **Figure 6.** Influence of the u/r ratio on hotspot detection. True positive (TP, upper panel) and
 359 false discovery (FD, lower panel) rates of hotspots called using a detection threshold of 2.5.
 360 The x axis indicates values of u for $r=10^{-8}$ (left panels), and values of r for $\mu=10^{-8}$ (right
 361 panels). Colors correspond to different values of the μ/r ratio. Asterisks show significant
 362 differences in percentages between comparisons (* prop.test p-value <0.05 , ** <0.01 ,
 363 *** <0.001).
 364
 365

366 ***Hotspot sharing between populations with different versus identical***
367 ***underlying recombination landscapes***

368 As expected for a comparison between two populations simulated with different
369 underlying recombination landscapes, the mean linear correlation (R^2 coefficient) between
370 the corresponding inferred landscapes was low, between 0.012 and 0.084, and similar to the
371 R^2 between the simulated landscapes (0.012-0.017) (Supplementary Table S2). A low
372 percentage of shared hotspots (around 8% with a calling threshold of 2.5) occurred by chance
373 between populations simulated with distinct underlying landscapes, with a SS of 20. Roughly
374 similar proportions of shared hotspots were found between the corresponding inferred
375 landscapes (with BP = 5), although these proportions were slightly overestimated (Figure 7,
376 see Supplementary Table S2 to see all conditions). A minority of the shared inferred hotspots
377 were TP, indicating that a non-zero fraction of truly shared hotspots is expected to be found
378 between species with different biological recombination landscapes.

379 Then we compared simulated populations sharing the same underlying landscape, in
380 order to check the ability of LDhelmet to recover similar recombination rates between
381 populations with independent coalescence histories. The correlations between simulated
382 landscapes were generally high for both low ($R^2 > 0.7$) and large N_e ($R^2 > 0.9$) conditions, but
383 the correlations between inferred landscapes were much lower, with $R^2 < 0.3$ and < 0.75 for N_e
384 = 25,000 and 250,000, respectively (Supplementary Table S2). The proportion of shared
385 hotspots called with a threshold of 2.5 followed the same trend: it was high between simulated
386 landscapes ($> 80\%$) and much lower between inferred landscapes ($< 50\%$) (Figure 7,
387 Supplementary Table S2). Thus, one can expect LDhelmet to detect a moderate to low fraction
388 of shared hotspots even between species truly sharing a common recombination landscape,
389 depending on population size and sample size (and also hotspot definition).

390



391

392 **Figure 7.** Expected and observed hotspot sharing between populations with different (left
 393 panel, following simulation framework from Supplementary Figure S3 A)) or identical (right
 394 panel, following simulation framework from Supplementary Figure S3 B) underlying
 395 landscapes. Mean proportion of shared hotspots between pairs of simulated (expected
 396 proportion, orange bars) and pairs of inferred (observed proportion, green bars) recombination
 397 landscapes as a function of N_e (i.e. 25,000 and 250,000, x axis). Only shown here are
 398 simulations with $SS = 20$, $BP = 5$, hotspots detection threshold = 2.5. The proportion of shared
 399 simulated and inferred hotspots for all combinations of parameters and for populations sharing
 400 or not the same underlying landscape are shown in Supplementary Table S2.

401

402 Populations simulated with the same underlying landscape that underwent a
 403 bottleneck or an admixture event also showed reduced hotspot sharing between inferred
 404 landscapes, as compared to truly shared hotspots between simulated landscapes. The
 405 proportion of shared hotspots between pairs of simulated landscapes was similar to constant-
 406 size populations and did not vary substantially according to the time or the strength of the
 407 demographic event, while the proportion of shared inferred hotspots decreased for younger
 408 events. This proportion was overall lower than for constant-size populations, but it sometimes
 409 reached, or even exceeded, the constant- N_e reference when events were ancient
 410 (Supplementary Figure S13 G, H).

411

412

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414

415

416 Discussion

417

418 ***Inferred LD-maps should be interpreted with caution***

419 Inference methods based on linkage disequilibrium provide an attractive way to
420 characterise genomic recombination landscapes from sequence data. As such, they promise
421 to become increasingly popular in empirical studies of eukaryotes. However, their ability to
422 accurately reproduce real recombination landscapes has not been specifically evaluated. It
423 should be recalled, however, that LD-based recombination maps are inferences, not
424 observations; biases and uncertainty must be quantified and taken into account when it comes
425 to interpreting the results. Here, we modelled the biological characteristics of a particularly
426 well-documented recombination landscape, that of humans, as a basis for assessing the
427 impact of methodological and species-specific demographic and evolutionary parameters on
428 the performance of the LDhelmet method. Our results send a message of caution regarding
429 the reliability of reconstructed recombination maps and hotspot location.

430 Indeed, we show that the recombination landscapes inferred with LDhelmet differ from
431 real landscapes, sometimes substantially, with Spearman rank correlation between simulated
432 and inferred 2.5 kb windows sometimes getting as low as 0.7 (Figure 2A, Supplementary
433 Figure S11A). Hotspot detection is a particularly tricky and error-prone task: while up to 85%
434 of true hotspots can be detected in the most favourable situations ($N_e = 250,000$, $SS = 20$, BP
435 $= 5$, threshold = 2.5), the FDR ranged from 19% to 82% (Figure 3, Figure 4B and C,
436 Supplementary Figure S9) according to the type of data and parameters used, meaning that
437 in many cases a majority of the detected hotspots are incorrect calls. These discrepancies
438 lead to a reduction in the apparent overlap in hotspot location between species/populations
439 with identical recombination landscapes, while in turn inflating apparent hotspot sharing in
440 populations with divergent landscapes (Figure 7, supplementary Table S2). These results
441 were obtained with recombination landscapes of simulated populations with constant effective
442 sizes, and with perfectly phased data. *In reality, empirical data needs to be phased, and the
443 phasing process can be prone to errors. Our analyses suggest that the typical error rate of
444 statistical phasing methods such as Shapeit4 is relatively low (~ 6.7% in our simulations) and
445 only marginally affects the performance of LDhelmet in terms of sensitivity and hotspot sharing
446 (Supplementary Figure S10), which is quite reassuring. Moreover, studied populations often
447 hide complex demographic histories that are known to impact the power to correctly infer
448 recombination rates (Dapper and Payseur 2018, Samuk and Nook 2021). We showed that
449 recent bottleneck and admixture events tend to decorrelate simulated and inferred
450 landscapes, decrease the TPR and increase the FDR, thus increasing the difficulty to call*

451 shared hotspots between populations sharing the same underlying landscape (Figure 5,
452 Supplementary Figure S13). The significant impact of non-equilibrium demographic histories
453 illustrated by our simulations provides additional motivation to characterise these histories in
454 comparative studies of recombination landscapes. These results also provide a qualitative
455 assessment of the impact of linked selection, whose effects may be similar to a local reduction
456 in N_e (i.e. purifying selection), or to the maintenance of anciently diverged alleles (i.e. balanced
457 selection, possibly involving structural variants such as chromosome inversions). If neglected,
458 these effects might mislead biological interpretations regarding the evolutionary conservation
459 of recombination maps.

460 In a study of the short time-scale dynamics of recombination landscapes based on
461 LDhelmet, Shanfelter et al. (2019) found only 15% of shared hotspots between two recently-
462 diverged populations of threespine stickleback. A greater overlap in hotspot location was a
463 *priori* expected given that this species lacks a functional PRDM9 protein, which is responsible
464 for the rapid turnover of recombination landscapes in mammals (Axelsson et al. 2012; Paigen
465 and Petkov 2018). The authors suggested that a new mechanism of recombination hotspot
466 regulation, different from the two already described in the literature, might be at play in this
467 teleost species. In the light of our results, however, one cannot exclude that the strong
468 divergence between the two reconstructed landscapes is due to a lack of power of the method
469 in the first place. While the sample size of both fish populations was at least 20 individuals, θ
470 was about 0.002, similar to our simulated conditions with a low N_e . Under these conditions, a
471 high FDR and a low proportion of shared hotspots can be expected even if the true underlying
472 maps are identical (Supplementary Figure S9, Supplementary Table S2).

473 It should be recalled that real data sets typically carry less signal and more noise than
474 simulated data sets, meaning that our assessment of the reliability of LDhelmet might be an
475 overoptimistic one. In particular, our data sets are immune from sequencing errors or mapping
476 errors, all of which presumably make the problem of recombination map inference an even
477 harder one.

478

479 ***Guidelines for population-based inference of recombination maps***

480 Our study revealed that whatever the parameters used, the inference of recombination
481 rates by LDhelmet is more reliable for species with large as compared to small effective
482 population size (Figure 4, 7, Supplementary Figure S9, S11). This might be expected since
483 long-term N_e determines the amount of nucleotide diversity ($\theta=4N_e\mu$, Watterson 1975), so that
484 a higher N_e results in a higher SNP density and a finer scale characterization of the
485 recombination rate variation along the genome. Moreover, a higher effective size greatly

486 corrects the general tendency of LDhelmet to overestimate the ρ value, especially for low and
487 high recombination rates (Supplementary Figure S6, Singhal et al. 2015; Booker et al. 2017).
488 Thus, when studying species with heterogeneous effective population sizes in nature, it is
489 recommended to select populations with the largest N_e , for which genetic diversity is greater.
490 The question is then: how to obtain a good-quality recombination map when dealing with low
491 N_e species? The sampling effort also determines, to a lesser extent, the polymorphism level
492 of the dataset (Supplementary Figure S5), improving the accuracy of the inference (Figure 2,
493 3 Supplementary Figure S9, S11). A sample size of 20 is recommended based on our
494 simulations. Moreover, as previously mentioned (Chan et al. 2012; Singhal et al. 2015), the
495 block penalty parameter of LDhelmet, which determines the resolution level of the inferred
496 landscape, also influences the length of the inferred map (*i.e.* a higher BP tends to mitigate
497 the tendency of LDhelmet to overestimate the map length) and the number of detected
498 hotspots (Supplementary Figure S4, S8). A small BP, that allows more fine-scale changes in
499 the inferred ρ value, should be used to detect recombination hotspots. The ability of LDhelmet
500 to faithfully reflect the fine-scale variation of real recombination landscapes is of great
501 importance when it comes to detecting recombination hotspots. To this purpose, the threshold
502 used to decide which region is defined as a “hotspot” is a key parameter that determines the
503 level of detection stringency. If the chosen value is not appropriate, LDhelmet will detect false
504 positives while also missing true hotspots (Supplementary Figure S9). This threshold should
505 thus be adapted to the species studied, using a less stringent threshold in species with lower
506 genome-wide average recombination rate.

507 Other intrinsic biological variables influence the ability to produce a faithful
508 recombination map, such as the μ/r ratio, which in part determines the power to measure ρ at
509 a fine-scale. The among-species variations in genome-average recombination rate r is well
510 documented, ranging from 0.01 to 100 cM/Mb in animals and plants, with vertebrate taxa
511 displaying an average r around 1 cM/Mb (Stapley et al. 2017). As previously mentioned, high
512 and low recombination rates tend to be overestimated by LDhelmet, thus the average r of the
513 studied species is obviously a key parameter to account for. The mutation rate μ also has a
514 key impact on the performance of LDhelmet, since ancestral recombination events can only
515 be detected if properly tagged by flanking mutations. The variation in μ across taxa, and
516 consequently the ratio of μ/r , are much less well known than the variation in r . This ratio, which
517 does not depend on the effective size of the population, is about 1 in humans, which means
518 that two recombination events are separated by one mutation on average. A ratio in favour of
519 mutations ($\mu/r > 1$) will improve the signal, increasing the TP rate and reducing the FD rate
520 (Figure 6, Supplementary Figure S12). But ultimately the performance of LDhelmet is

521 conditioned by r , as low r values provide less power to detect the recombination events, even
522 with $\mu/r = 10$. Thus, the mutation to recombination rate ratio is crucial to build a non-biased
523 recombination map. When studying a species for which it appears that this ratio is not
524 favourable, a high rate of false positive hotspots is expected from the inferred population
525 recombination landscape (Figure 6), making it difficult to compare maps between closely
526 related species in a meaningful way.

527

528 **Limitations**

529 The aim of our study was to determine the limits of LD-based methods in inferring
530 biologically realistic recombination landscapes. For this purpose, we used the Pratto et al.
531 (2014) ChIP-seq DMC1 data set to build human-like recombination landscapes including both
532 broad and fine scale variation, reflected by the presence of numerous recombination hotspots
533 of different intensities (Supplementary Figure S2, Myers et al. 2005, 2006; Pratto et al. 2014).
534 We therefore assumed that the distribution of DSB reflects the distribution of crossing overs,
535 which is not true for sure. For instance, hotspots were here placed without taking into account
536 the existence of genomic features that correlate with the recombination rate, such as genes
537 and promoter-like regions, GC-rich regions, CpG islands, and polymorphic regions, which can
538 explain why a very intense and narrow hotspot is never found within a region of near zero
539 recombination. The sensibility of LD-based methods with respect to this architecture was not
540 tested. We did not take into account the effect of gene conversion on the dissipation of LD in
541 high-recombining regions. While recent methods aim to distinguish between crossing-over
542 (CO) and non-crossing-over (NCO) events (heRho, Setter et al. 2022), they do not (yet)
543 account for the small-scale heterogeneity of recombination rates, and so are not really
544 applicable when it comes to differentiate hotspots and NCO. Our simulated data were perfectly
545 polarised, without missing or low-quality genotypes, which can't be the case when dealing
546 with empirical data. We simulated phasing errors in order to assess the robustness of
547 LDHelmet to this problem. However, we estimated the phasing error rate of Shapeit4 from our
548 simulated data which lack most of the biases found in empirical data, thus probably
549 underestimating the typical phasing error of this method.

550 Finally, we don't know if these simulated landscapes are representative of the diversity
551 of recombination landscapes that exist in the living world (*i.e.* PRDM9-dependent vs
552 independent landscapes, hotspot-free landscapes...). Indeed, it is likely that the high
553 complexity of the human recombination landscape is not a universal feature in the animal
554 kingdom. Singhal et al. (2015) used LDHelmet for building the recombination map in two
555 species of birds, the zebra finch and the long-tailed finch, that lack a full-length PRDM9 gene

556 copy and diverged about 2.9 Myr. The sample size for both populations was about 20
557 individuals, and θ (~ 0.01) was about ten times higher than in apes or the threespine
558 stickleback (Shanfelter et al. 2019), thus corresponding to our high N_e simulation conditions.
559 Singhal et al. (2015) found 73% of shared hotspots between the two finch species, which is
560 a higher rate of hotspot sharing than in any of the scenarios we simulated. The median
561 estimated recombination rate was 0.14 cM/Mb in both species of finch, which is seven times
562 lower than the genome-wide average recombination rate in humans (about 1 cM/Mb, Jensen-
563 Seaman et al. 2004). Combined with the strong polymorphism in those species, we may
564 suppose that birds possess less complex recombination landscapes than humans or
565 compared to what we simulated, which might explain why LDhelmet recovered such a high
566 percentage of shared hotspots in this study.

567

568

569 **Conclusion**

570

571 In the past few years, we have seen a growing interest in recombination rate estimation
572 in functional and evolutionary genomics. Indirect, LD-based approaches raise methodological
573 challenges that are addressed by sophisticated methods such as LDhat or LDhelmet, the
574 reliability of which is still poorly characterised. Our study provides guidance to users of these
575 methods based on the characteristics of their species, and calls for caution when it comes to
576 interpreting fine-scale differences in recombination rates between species. Extending this
577 approach to a more diverse set of underlying recombination landscapes would help
578 characterise further the reliability of these methods and their range of applicability across data
579 sets and taxa.

580

581

582 **Materials and Methods**

583

584 Our approach separately considers three different layers of information that are
585 involved in the study of recombination landscapes (Figure 1). The first layer that we call the
586 “underlying” recombination landscape corresponds to the true biological distribution of
587 recombination rate (r) across the considered genome. We here used experimental
588 measurements from human studies to model and generate the “underlying” landscapes. The
589 second layer, the population recombination landscape, describes the genomic location of
590 recombination events that occurred during the history of the sample. We used coalescent

591 simulations to produce these population recombination landscapes, thereafter called
592 “simulated” landscapes. Simulated landscapes differ from the underlying landscape due to
593 the stochasticity of the coalescent process, which is inversely proportional to N_e . The third
594 layer, called the “inferred” landscape, corresponds to the output of LDhelmet, *i.e.* an estimate
595 of the population recombination rate between adjacent SNPs. In total we generated five
596 independent replicates of underlying landscapes, and for each of them up to 10 simulated and
597 inferred landscapes [under various demographic scenarios](#) (Figure 1, Supplementary Figure
598 S3A).

599

600 ***Underlying landscapes***

601 Underlying recombination landscapes were first generated to reproduce the features
602 of the human recombination landscape. These include large-scale variation in the mean
603 background recombination rate and fine-scale variation reflecting the presence of hotspots
604 with varied intensities. Meiotic DSB are the major determinant of crossing over (CO) location
605 along the genome (Li et al. 2019; Pratto et al. 2014). We used the high-resolution map of
606 meiotic DSB obtained using ChIP-seq DMC1 in 5 non-related human genomes (Pratto et al.
607 2014) to define the genome-wide distribution of recombination rates in our simulations. The
608 five individuals analysed in Pratto et al. (2014) carried different PRDM9 genotypes totaling
609 about 40,000 hotspots per individual, with distinct genotypes having different sets of DSB
610 hotspots. For each individual, a gamma distribution was fitted to the empirical distribution of
611 hotspot intensity measured by ChIP-seq DMC1 with the R package *figdistribplus* (Delignette-
612 Muller and Dutang 2015). Extreme ChIP-Seq intensity values (>500) lying above the 97.5th
613 quantile and likely representing technical artefacts were removed. Remaining values were
614 rescaled to 0-100, so as to transform ChIP-Seq intensity values into quantities reflecting the
615 range of recombination rates reported in cM/Mb across the human genome (McVean et al.
616 2004, 2005). This conversion assumed a linear relation between DMC1 activity and CO
617 frequency (Pratto et al. 2014). We then removed null values and replaced them with small but
618 non-null values (0.001), so that the genome-wide mean recombination rate equaled a target
619 average (*e.g.* 1 cM/Mb). A Gamma distribution was fitted to these transformed empirical values
620 separately for each of the 5 individuals, before averaging shape and scale parameters across
621 individuals. Targeted genome-wide average value was set to either 1 cM/Mb or 3 cM/Mb,
622 respectively reflecting the average centro-chromosomal and subtelomeric rates in humans.
623 Underlying landscapes of 1 Mb length were built by randomly drawing independent
624 recombination rate values from the fitted distribution and assigning these to non-overlapping
625 windows of 500 pb. Values in the first 500 kb were drawn from a distribution of mean 1 cM/Mb,

626 while values in the last 500 kb were drawn from a distribution of mean 3 cM/Mb. Our approach
627 thus mimics both the large scale variation in recombination rate existing in humans (Nachman,
628 2002; Myers et al. 2005; Buard and de Massy 2007; Pratto et al. 2014) and the nearly absence
629 of recombination events outside hotspots (96% of CO occur in hotspots in mice, Pratto et al.
630 2014; Li et al. 2019). In total, 5 underlying landscapes were generated (mean $r = 2$ cM/Mb),
631 which can be considered as independent replicates driven from the same distribution (*i.e.*
632 regions from different chromosomes of the same species, or orthologous chromosome region
633 from closely related species).

634

635 ***Simulated landscapes***

636 For each of the 5 underlying landscapes, 10 simulated landscapes were generated via
637 coalescent simulations using the program MSPRIME (v0.7.4, Kelleher et al. 2016), varying
638 the constant effective population size ($N_e = 25,000$ or $250,000$) and the sample size (SS=10
639 or 20) and setting the mutation rate to $\mu = 10^{-8}$. These sets of simulation parameters were
640 combined with three values of the Block Penalty (BP) parameter of the LDhelmet program
641 (see below), resulting in twelve conditions tested. For each combination of parameters, ten
642 population samples were simulated, to generate independent replicates of the coalescent
643 history (Figure 1A, Supplementary Figure S3).

644 Populations undergoing bottleneck and admixture events were also simulated with
645 MSPRIME, using one of the five underlying landscapes. The sample size parameter was set
646 to 20, and the N_e of the ancestral and present-day population was set to 250,000. The
647 simulated bottleneck scenarios varied according to the timing of the bottleneck event ($t_b = 500$,
648 5,000, 50,000 generations ago) and the N_e of the population during the bottleneck ($N_b = 2,500$,
649 25,000). The duration of the bottleneck was fixed to 1,000 generations. The admixture
650 scenarios varied in terms of the timing of the admixture event between the derived populations
651 1 and 2 ($t_a = 500$, 5,000, 50,000 generations ago). The time of split of the ancestral population
652 (0) into two derived population 1 and 2 (t_{split}) was set to $10 * N_e$ generations. For each bottleneck
653 and admixture scenario, ten replicated populations were simulated (Figure 1A,B).

654 A VCF file was generated with MSPRIME for each simulated population (Figure 1A,
655 Supplementary Figure S3), which contains the genotypes of variants that segregate in the
656 population sample consisting of $2n$ sequences (with n being the number of diploid samples)
657 following the given underlying recombination landscape.

658 The impact of phasing errors on the inference of recombination rates was also
659 assessed. Two replicate VCFs, simulated using the same underlying landscape, were
660 manually dephased and then phased using Shapeit 4.2.2 (Delaneau et al., 2019). The phasing

661 error rate was computed using the --switch-error option of VCFtools 0.1.17 (Danecek et al.
662 2011 ; using the original phased VCF as a reference). Phasing error rates of 2, 4, 6, 8 and
663 10% between heterozygous positions of the two original phased VCFs were then randomly
664 generated, to produce five independent replicate VCF for each phasing error rate value.

665

666 ***Inferred landscapes***

667 Recombination rates were estimated for each of the simulated samples with LDhelmet
668 (v1.19, Chan et al. 2012, Figure 1). Briefly, LDhelmet uses phased sequence data to infer the
669 ρ parameter locally, using likelihood computation between pairs of SNPs and then averaging
670 over 50 consecutive variants to obtain a composite likelihood. The ρ parameter is inferred with
671 a reversible-jump Markov Chain Monte Carlo algorithm using a step function applied to every
672 window of 50 consecutive SNPs and determined by three parameters: the number of change-
673 points, the locations of changes, and the recombination rate value of each constant fragment
674 between two changes. We used VCFtools 0.1.17 (Danecek et al. 2011) and the vcf2fasta
675 function of vcflib (<https://github.com/vcflib/vcflib>) to convert the SNP data obtained from
676 MSPRIME simulations into the input format to LDhelmet, consisting of FASTA sequences of
677 each individual haplotype. Ancestral states defined as the reference allele of each variant
678 were also used as inputs. Each simulated replicate was analysed with LDhelmet using the
679 following parameters. The haplotype configuration files were created with the find_conf
680 function using the recommended window size of 50 SNPs. The likelihood look-up tables were
681 created with the table_gen function using the recommended grid for the population
682 recombination rate (ρ /pb) (*i.e.* ρ from 0 to 10 by increments of 0.1, then from 10 to 100 by
683 increments of 1), and with the Watterson $\theta = 4N_e\mu$ parameter corresponding to the condition
684 analysed. The Padé files were created using 11 Padé coefficients as recommended. The
685 Monte Carlo Markov chain was run for 1 million iterations with a burn-in period of 100,000 and
686 a window size of 50 SNPs. An important parameter to LDhelmet is the block penalty (BP),
687 which determines the number of change-points, and thus the variance of the inferred
688 recombination rates at a fine scale (*i.e.* smaller block penalty values correspond to a lower
689 penalty for background rate changes, and thus generate more heterogeneous recombination
690 landscapes). For each simulated combination of N_e and SS for populations with constant size,
691 the block penalty was set to either 5, 10 or 50, and for the simulated populations undergoing
692 bottleneck or admixture event, as for the "phase-error" datasets, the block penalty used was
693 set to 5. Finally, the population recombination rates between each SNP pair were extracted
694 with the post_to_text function, and were reported in $\rho=4N_e r$ per pb unit.

695 The reliability of the inferences was evaluated in various ways. For each combination

696 of N_e , SS, BP parameters and demographic scenarios simulated, the inferred, simulated and
697 underlying landscapes were compared, in order to assess the ability of LDhelmet to reliably
698 infer the true biological landscape (Figure 1, Supplementary Figure S3A, and see below
699 Hotspot detection and Statistical Analysis). In order to evaluate the convergence of LDhelmet
700 inferences across replicate runs, LDhelmet was run 10 times, for the 12 combinations of the
701 parameters N_e , SS and BP, on two independently simulated VCF files from constant-size
702 populations sharing the same underlying landscape (Figure 1A, Supplementary Figure S3B).
703 Finally, the inferred recombination landscapes of pairs of populations sharing the same
704 underlying landscape were compared in order to assess the reproducibility of the LDhelmet
705 inference, *i.e.*, the expected variance between inferred maps in the absence of underlying
706 biological variation (Figure 1, Supplementary Figure S3B).

707

708 ***Variation in the μ/r ratio***

709 To explore the influence of variation in mutation and recombination rates on the
710 inference of recombination maps, two additional underlying landscapes were generated using
711 the same procedure, this time targeting a ten times higher (*i.e.* 20 cM/Mb) or ten times lower
712 (0.2 cM/Mb) mean recombination rate. Then, using one of the 5 underlying landscapes ($r \sim$
713 10^{-8} M/pb) and the 2 newly generated landscapes with mean $r = 10^{-7}$ and 10^{-9} M/pb,
714 respectively, sets of simulations were run with a μ/r ratio of 0.1, 1 and 10. This was achieved
715 by fixing μ to either 10^{-9} , 10^{-8} or 10^{-7} , while keeping a fixed $N_e = 100000$ and SS = 20
716 (Supplementary Table S1). For each of the tested combinations of μ and r , 10 populations
717 were simulated. These simulated landscapes were inferred with LDhelmet, using a block
718 penalty of 5.

719

720 ***Hotspot detection***

721 Underlying and simulated landscapes were first converted into population
722 recombination rate landscapes by scaling them by $4N_e$. Underlying, simulated and inferred
723 landscapes were then smoothed at a 500 bp and 2500 bp resolution using the Python package
724 *scipy.stats*. The former corresponds to the underlying landscape resolution, and the latter to
725 a trade off between the density of segregating sites and the resolution often used in the
726 literature. For the different combinations of N_e , SS and BP of the constant-size populations
727 simulated with the 5 underlying landscapes, a mean simulated landscape and a mean inferred
728 landscape were generated by averaging recombination rates across replicates.

729 Recombination hotspots of the underlying, simulated and inferred landscapes were
730 called by comparing local vs surrounding recombination rates at each genomic window. A

731 hotspot was defined as a window of 2.5 kb with an average recombination rate either 2.5, 5
732 or 10 times higher than the 50 kb flanking regions (excluding the focal window). Hotspot
733 locations were then compared among landscapes using the same threshold values (Figure
734 1C)

735

736 **Statistical analyses**

737 Statistical analyses were run with R 4.0.3. The length of underlying, simulated and
738 inferred maps (L) was calculated at the 2.5 kb resolution using the formula:

$$739 \quad L = \sum (\rho \times win)/4N_e,$$

740 with ρ the population-scaled recombination rate, win the window size resolution used to
741 smooth the maps in bp, and N_e the effective size of the simulated population. Several
742 measures of the sensitivity, specificity, reliability, and repeatability of LDhelmet were
743 computed, using the mean simulated and inferred landscapes of the constant-size
744 populations, and replicates of simulated and inferred landscapes of the populations that
745 underwent bottleneck of admixture events. Spearman rank correlation coefficients were
746 calculated between the underlying and the corresponding simulated landscapes, between the
747 simulated and inferred landscapes, and pairwise Spearman coefficients among the 10
748 replicates inferred from the two simulated populations sharing the same underlying landscape.
749 True/false positive rates (TPR = TP/(TP+FN) ; FPR = FP/(FP+TN)), true/false negative rates
750 (TNR = TN/(TN+FP) ; FNR = FN/(FN/(TP+FN)), and true/false discovery rates (TDR =
751 TP/(TP+FP) ; FDR = FP/(TP+FP)) were calculated by comparing the simulated and inferred
752 landscapes. The mean pairwise linear correlation (R^2) and the proportion of shared hotspots
753 was calculated between the 5 underlying landscapes, and for each condition simulated with
754 a constant population size scenario, and for the three threshold values tested (*i.e.* 2.5, 5 and
755 10) between the simulated and inferred landscapes from the 5 different underlying landscapes,
756 as well as between the pairs of populations sharing the same underlying landscape.

757 The statistical analyses were performed using home-made R scripts available upon
758 request.

759

760

761 **Data, script and code availability**

762 The underlying landscapes, the main scripts used to generate the underlying
763 landscapes, run the simulations under the various demographic scenarios, infer the simulated
764 landscapes with LDhelmet, and call hotspots from the landscapes can be found at
765 https://github.com/marie-raynaud/Performance_LD_methods_recombination. The Singularity

766 container recipe built to run the simulations is available at:[https://github.com/marie-](https://github.com/marie-raynaud/Singularity-Recipes/tree/master/HotRec-Recipes)
767 [raynaud/Singularity-Recipes/tree/master/HotRec-Recipes](https://github.com/marie-raynaud/Singularity-Recipes/tree/master/HotRec-Recipes). This recipe contains the
768 installation command lines of the required programs, the scripts used for the simulations, and
769 the five underlying landscapes used in our study. More scripts and data are available upon
770 request.

771

772

773 **Supplementary information**

774 [Supplementary Materials, containing Supplementary Figures and Tables are available at](#)
775 <https://doi.org/10.5281/zenodo.7544555>.

776

777

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783

784

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787

788

789 **Conflict of interest disclosure**

790 The authors declare no conflict of interest.

791

792

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794

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